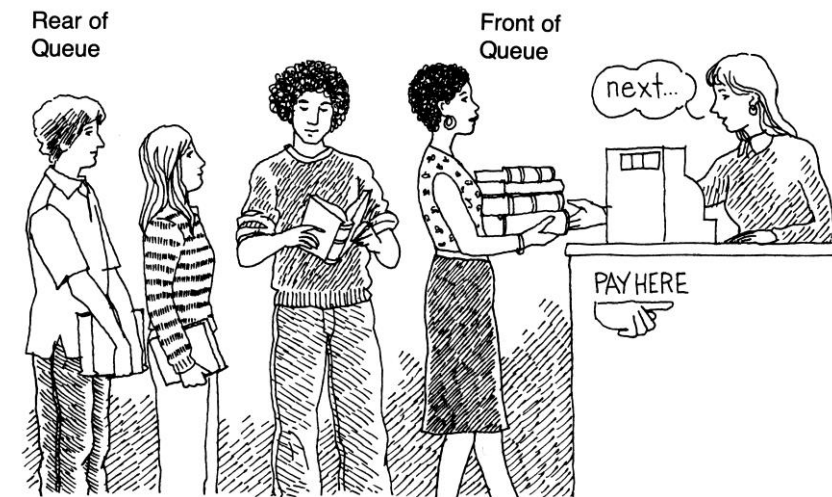


# Queue



# Queue ADT

---

- ▶ A **Queue** is a data structure that has two ends:
  - Elements are added at one end called “**rear**”.
  - And removed from the other end called “**front**”.
- ▶ Insertions and deletions follow **First-in First-out (FIFO)** scheme (principle).
  - It means that the element added last will be removed first.



# Queue ADT

---

## ➤ Main operations

- **enqueue(object)**: Insert element at **rear**.
- **object dequeue()**: Remove and returns element at **front**.

## ➤ Auxiliary operations

- **object front()**: returns front element without removing it.
- **integer size()**: returns number of elements stored.
- **boolean isEmpty()**: returns whether no elements are stored.

# Applications of Queues

---

## ➤ Direct

- Waiting lines.
- Access to shared resources.
- Hold jobs for a printer.
- The most common application is in client-server models
  - Multiple clients may be requesting services from one or more servers
  - Some clients may have to wait while the servers are busy
  - Those clients are placed in a queue and serviced in the order of arrival

## ➤ Indirect

- Auxiliary data structure for algorithms
- Component of other data structures

# Array-based Queue

- Add elements in an array  $Q$  of capacity(size)  $N$ .
- Two Variables:
  - *front* that points to the beginning of the Queue.
  - *rear* that points to the end of the Queue.



# Enqueue and Dequeue Algorithms

---

```
Algorithm Enqueue(Element):  
  if isFull then  
    throw Full Queue Exception  
  else  
     $Q[\textit{rear}] \leftarrow \textit{element}$   
     $\textit{rear} \leftarrow \textit{rear} + 1$ 
```

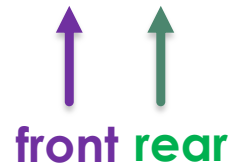
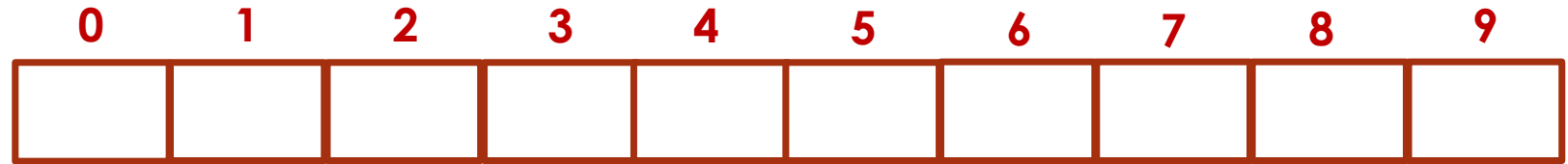
Run time:  $O(1)$

```
Algorithm Dequeue():  
  if isEmpty then  
    throw Empty Queue Exception  
  else  
     $\textit{item} \leftarrow Q[\textit{front}]$   
     $Q[\textit{front}] \leftarrow \text{Null}$   
     $\textit{front} \leftarrow \textit{front} + 1$   
  return item
```

Run Time:  $O(1)$

# Queue Operations - Example

- Queue Q, N=10



Enqueue (9)

{

if isFull Then

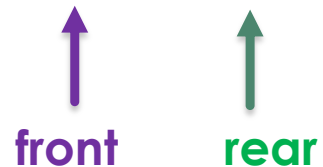
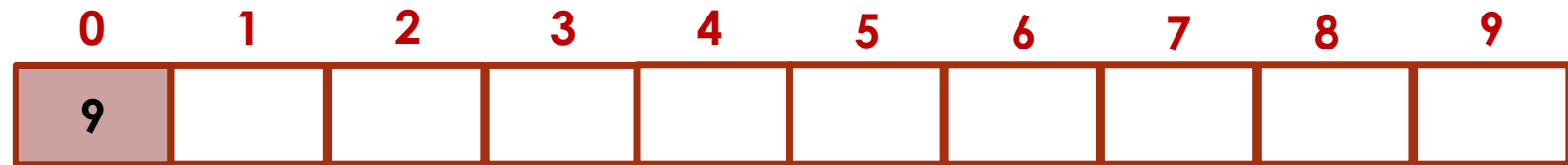
    "Queue is Full"

else

    Q[rear]=9

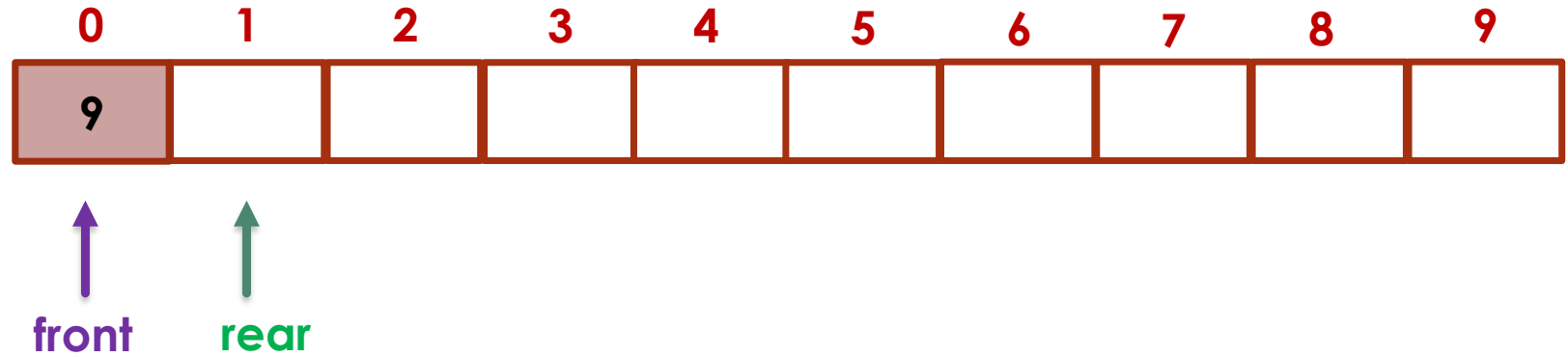
    rear=rear+1

}



# Queue Operations - Example

- Queue Q, N=10



**Enqueue (3)**

{

if isFull Then

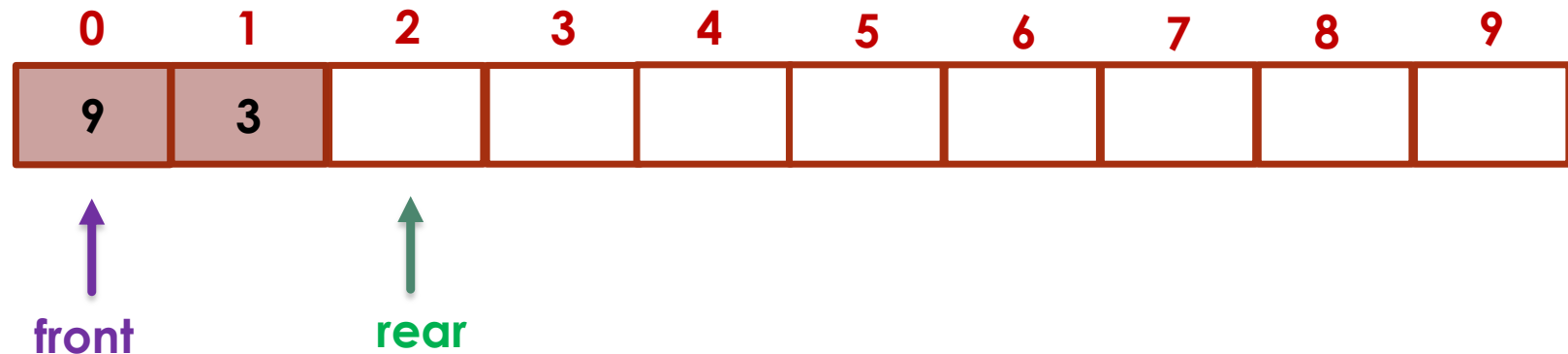
    "Queue is Full"

else

    Q[rear]=3

    rear=rear+1

}





# Queue Operations - Example

- Queue Q, N=10

Enqueue (5)

{

if isFull Then

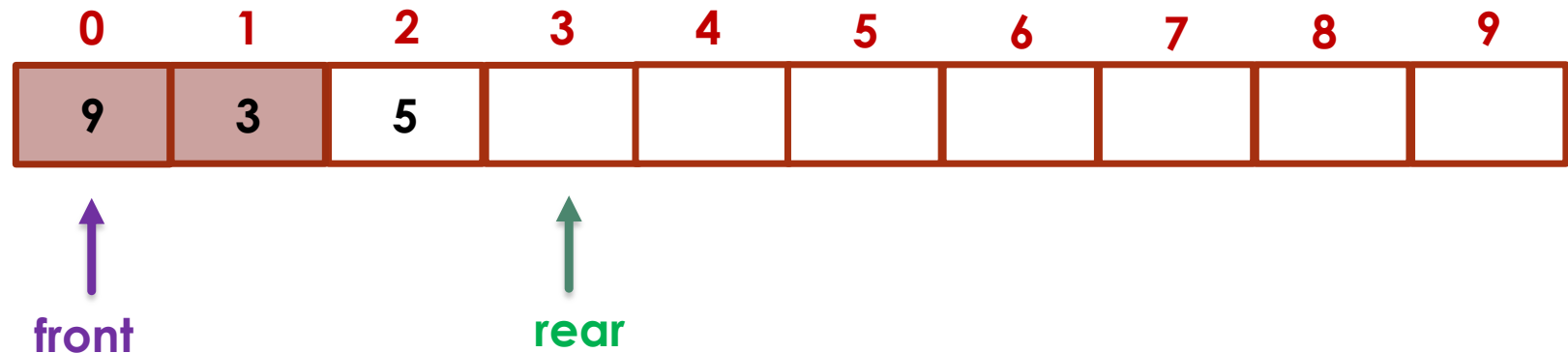
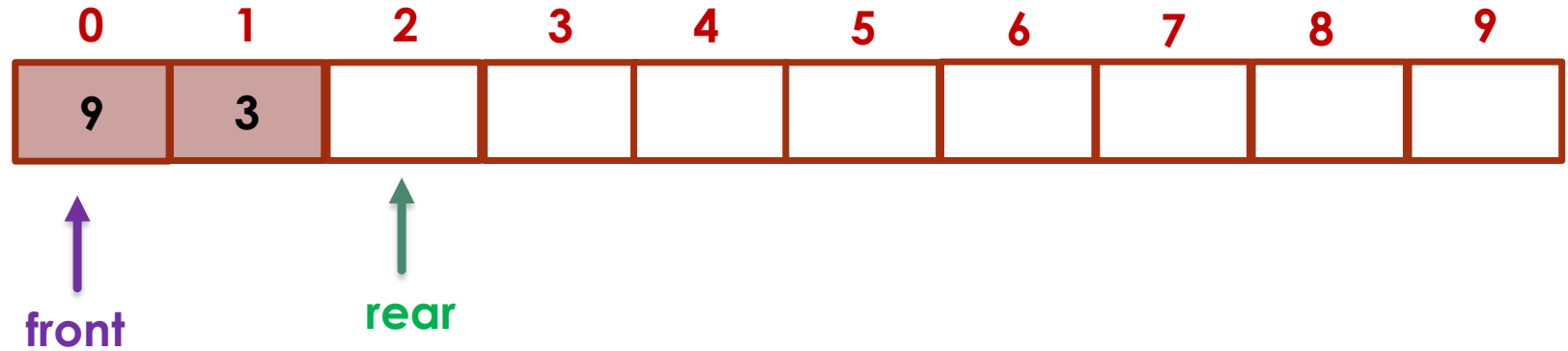
    "Queue is Full"

else

    Q[rear]=5

    rear=rear+1

}



# Queue Operations - Example

- Queue Q, N=10

**Dequeue ()**

{

if isFull Then

    "Queue is empty"

else

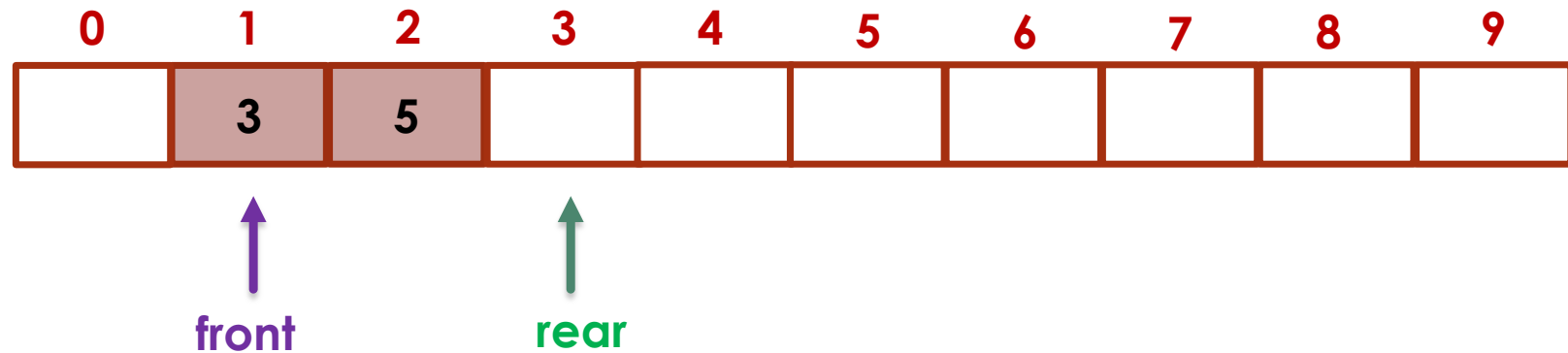
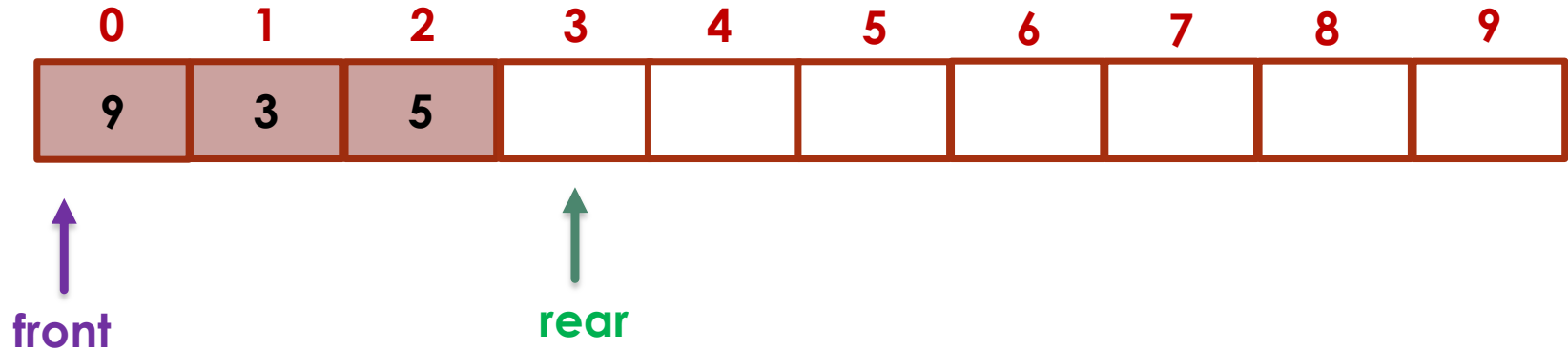
    item=Q[front]

    Q[front]=null

    front=front+1

    return item

}



# Queue Operations - Example

- Queue Q, N=10

**Dequeue ()**

{

if isEmpty Then

    "Queue is empty"

else

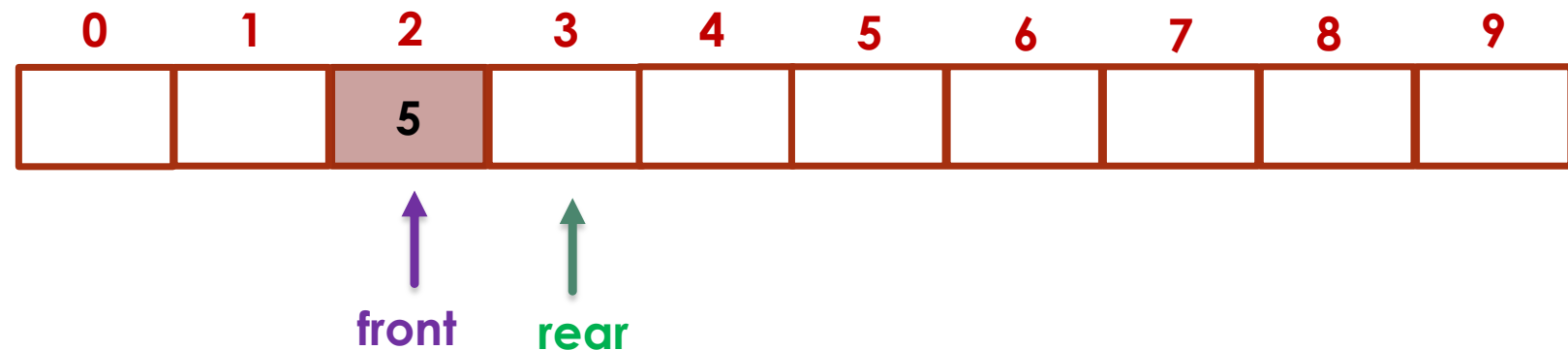
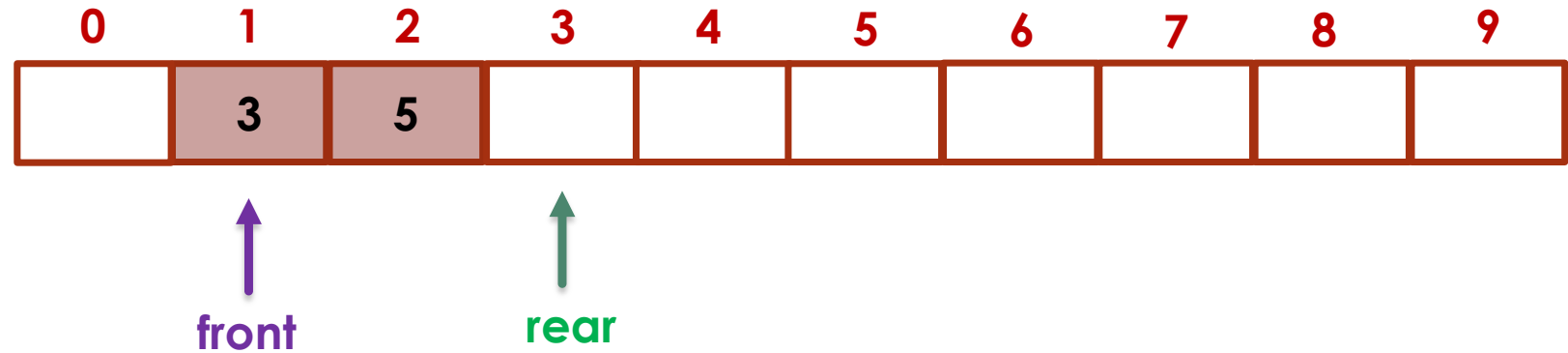
    item=Q[front]

    Q[front]=null

    front=front+1

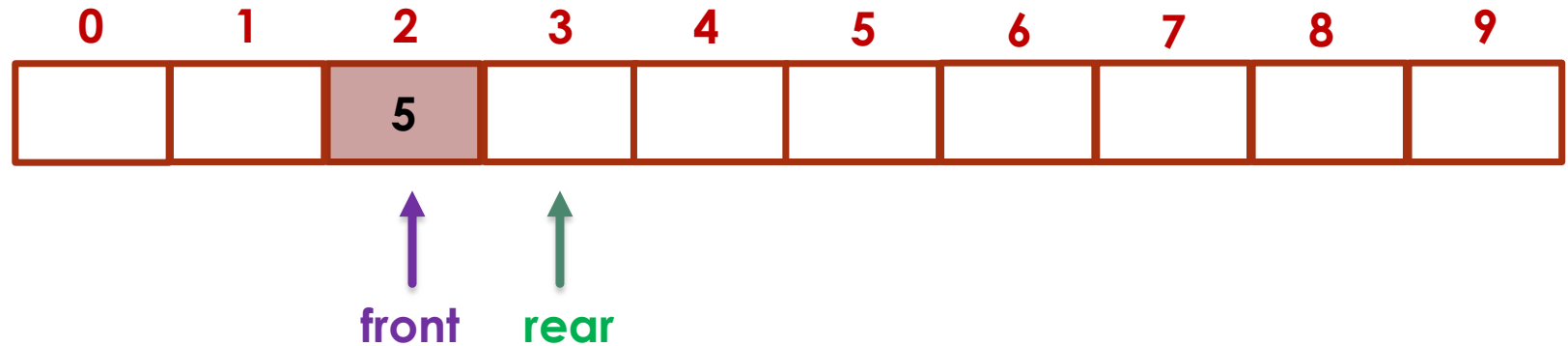
    return item

}



# Queue Operations - Example

- Queue Q, N=10



**Dequeue ()**

{

if isEmpty Then

    "Queue is empty"

else

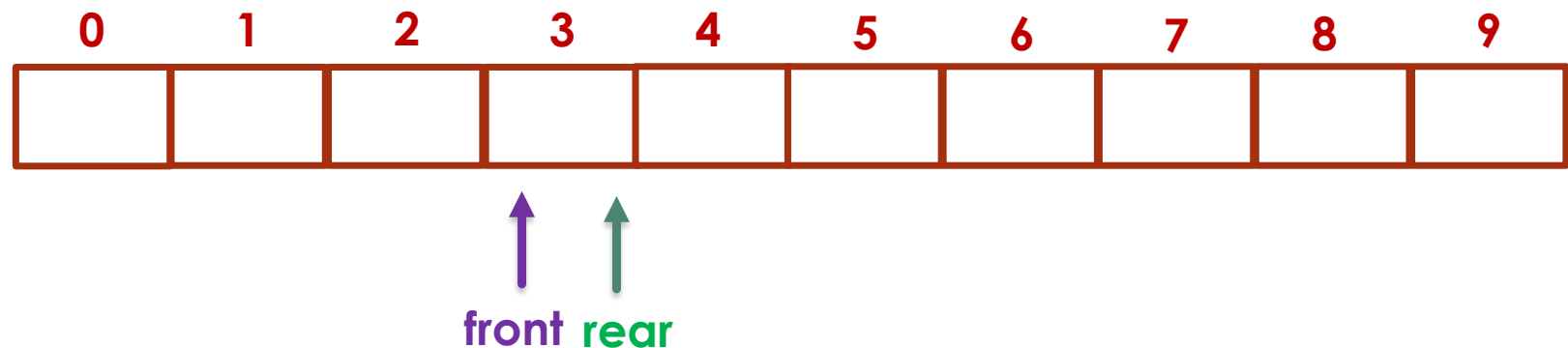
    item=Q[front]

    Q[front]=null

    front=front+1

    return item

}



# Queue Operations - Example

- Queue Q, N=10

Enqueue (8)

Enqueue (1)

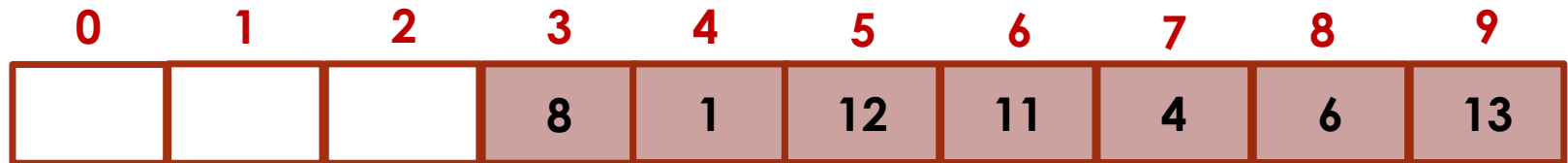
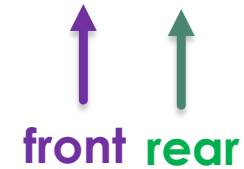
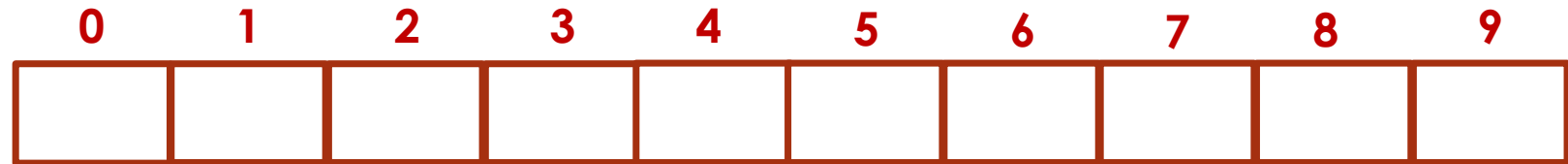
Enqueue (12)

Enqueue (11)

Enqueue (4)

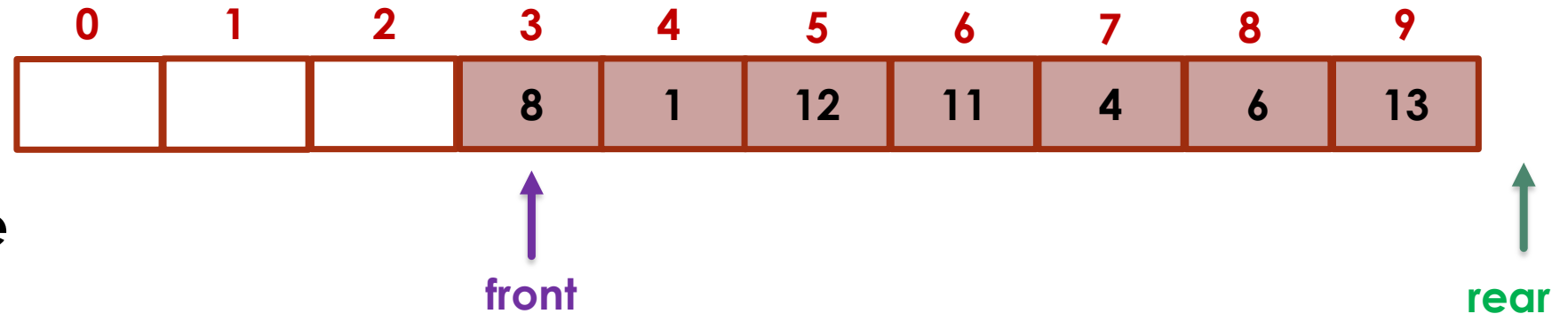
Enqueue (6)

Enqueue (13)



# Queue Operations - Example

- Queue Q, N=10



Now, let's add one more element **7**.

Enqueue (7)

```
{  
  if isFull Then  
    “Queue is Full”  
  else  
    Q[rear]=7  
    rear=rear+1  
}
```

What is the problem?

Once queue becomes full, we can not insert the next element even if there is a **space** in front of queue. **waste of memory in a Queue.**



# Circular Queue

*To Solve the waste memory in Queue.*

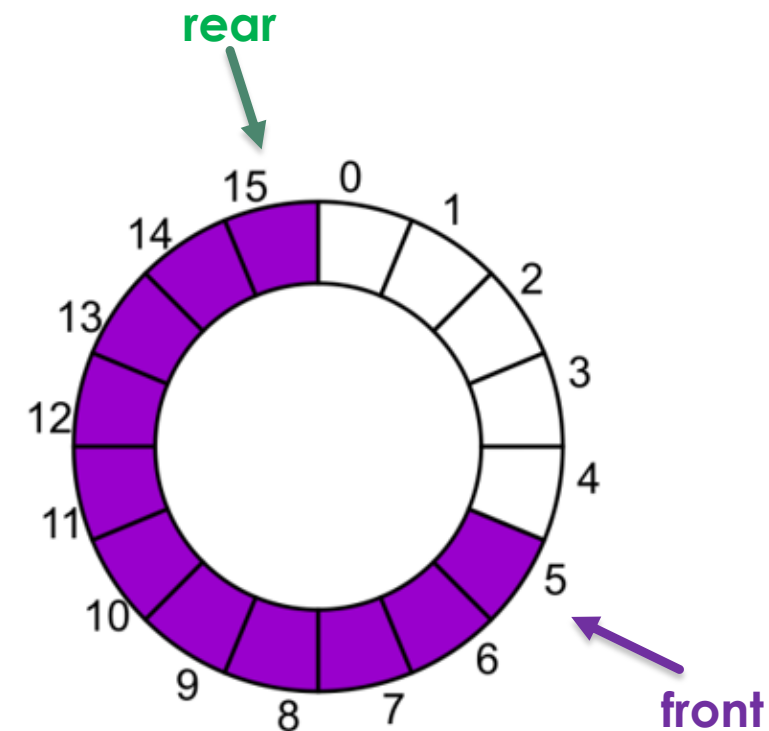
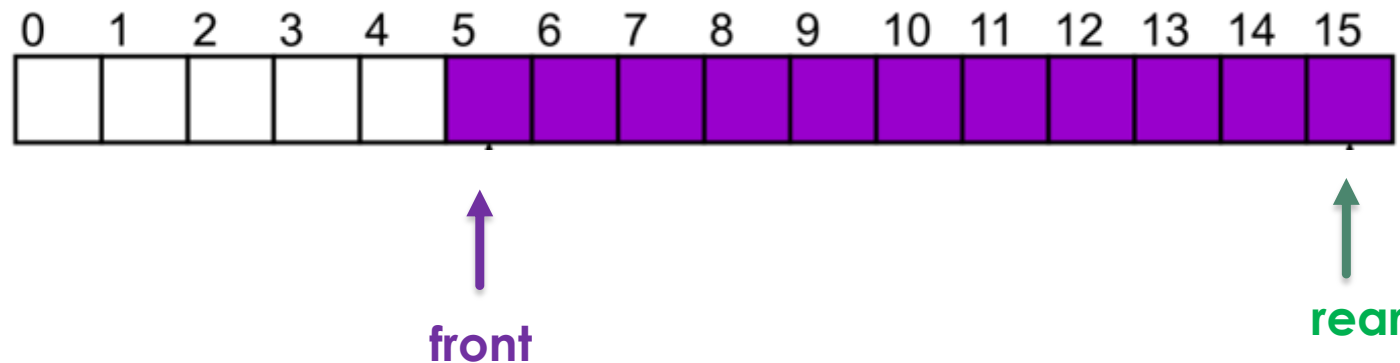
# Circular Queue

- Instead of viewing the array on the range 0, ..., 15, consider the indices being cyclic:

..., 15, 0, 1, ..., 15, 0, 1, ..., 15, 0, 1, ...

This is referred to as a circular array.

- view Q as a "circular array" that goes from Q [0] to Q [N-1 ] and then immediately back to Q [0] again.





# Enqueue and Dequeue Algorithms

---

```
Algorithm Enqueue(Element):  
  if isFull then  
    throw Full Queue Exception  
  else  
     $Q[\mathit{rear}] \leftarrow \mathit{element}$   
     $\mathit{rear} \leftarrow (\mathit{rear} + 1) \bmod N$ 
```

Run time:  $O(1)$

```
Algorithm Dequeue():  
  if isEmpty then  
    throw Empty Queue Exception  
  else  
     $\mathit{item} \leftarrow Q[\mathit{front}]$   
     $Q[\mathit{front}] \leftarrow \text{Null}$   
     $\mathit{front} \leftarrow (\mathit{front} + 1) \bmod N$   
  return item
```

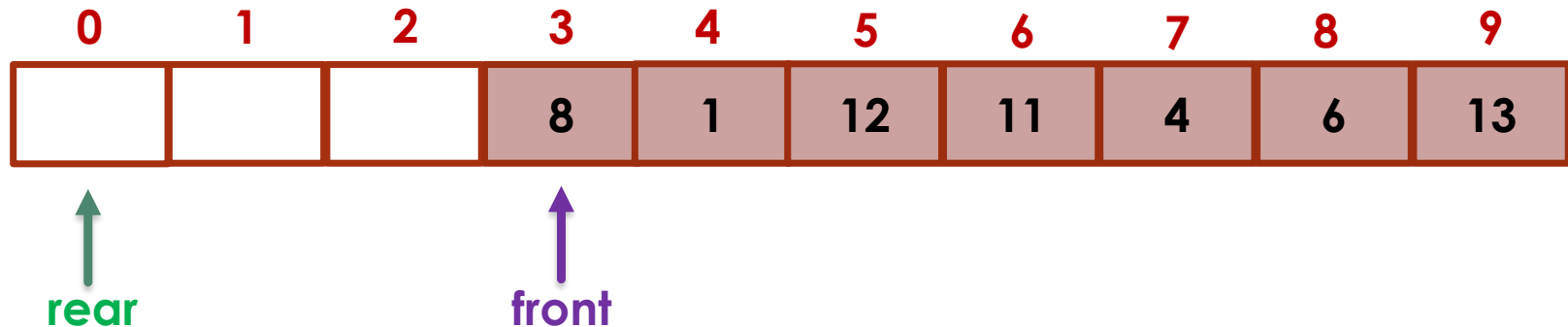
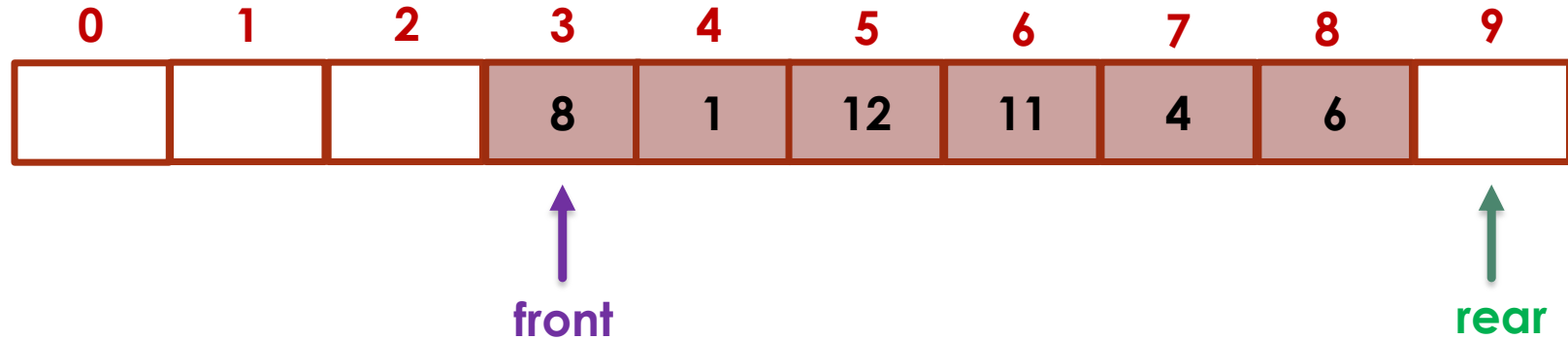
Run Time:  $O(1)$

# CQueue Operations - Example

- Queue Q, N=10

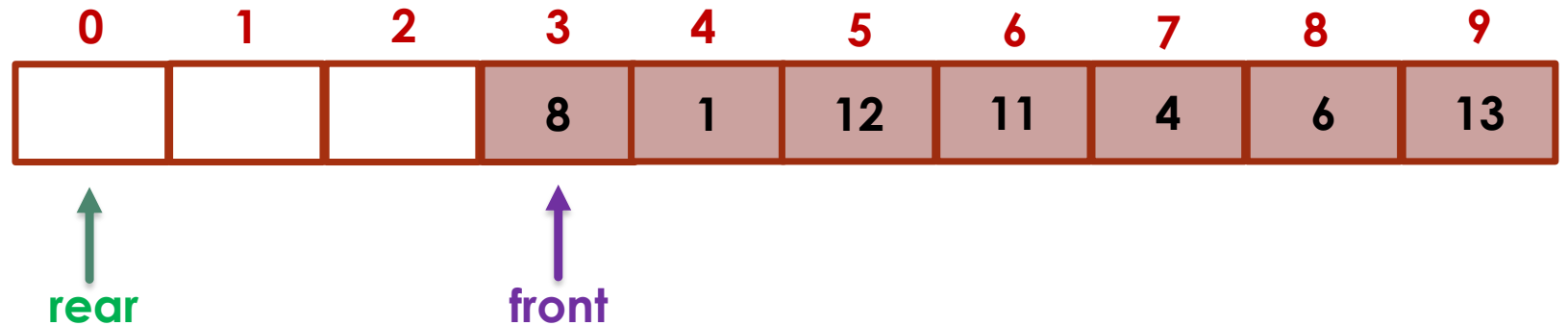
Enqueue (13)

```
{  
  if isFull Then  
    "Queue is Full"  
  else  
    Q[rear]=13  
    rear=(rear+1) mod N  
}
```



# CQueue Operations - Example

- Queue Q, N=10



Enqueue (7)

{

if **isFull** Then

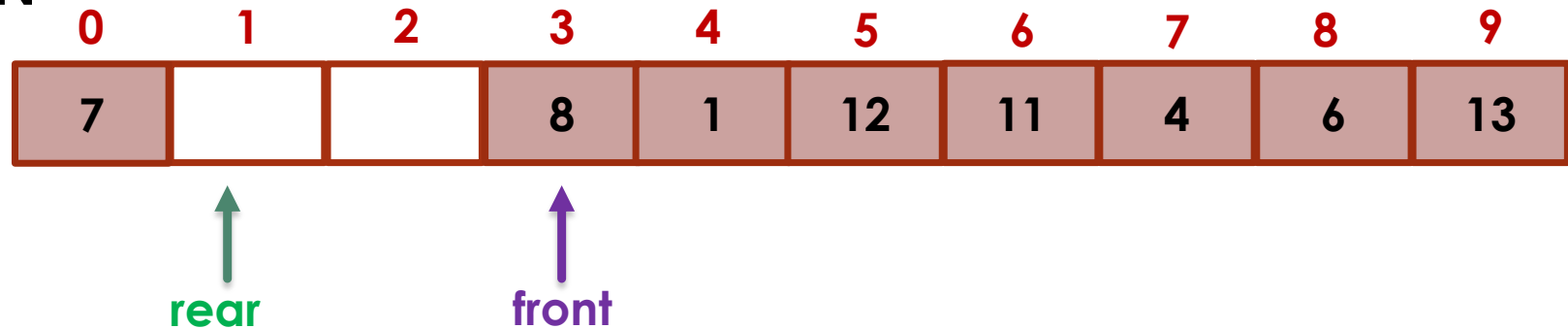
    "Queue is Full"

else

    Q[rear]=7

    rear=(rear+1) mod N

}



# CQueue Operations - Example

- Queue Q, N=10

Dequeue ()

{

if **isEmpty** Then  
    "Queue is Empty"

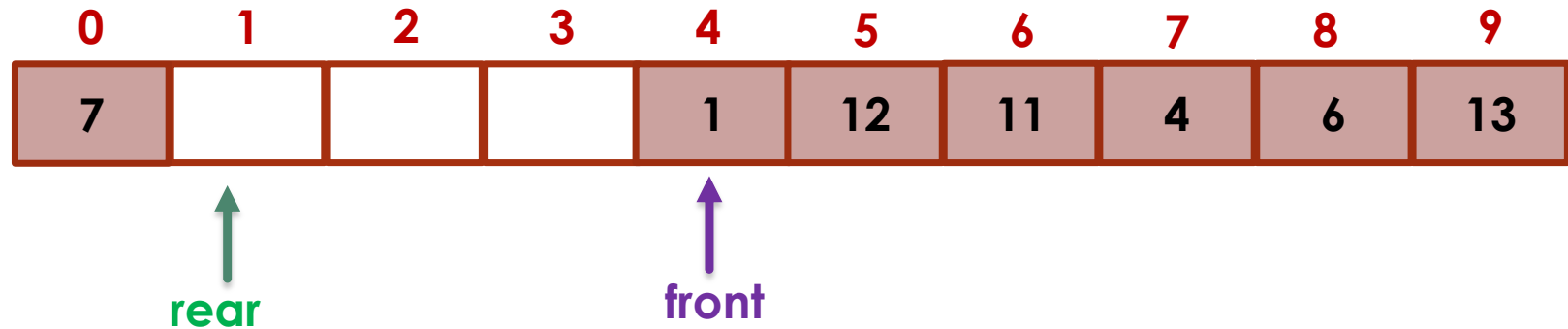
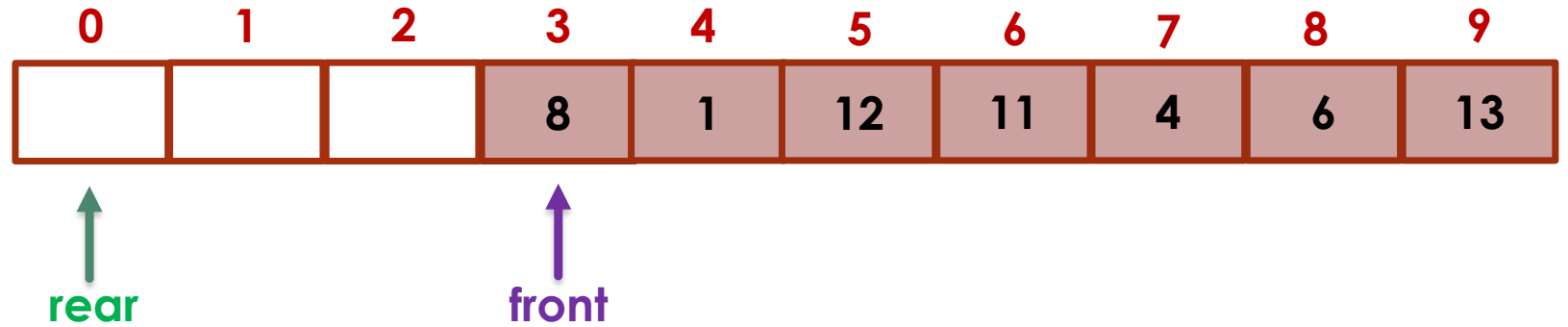
else

    item=Q[front]

    Q[front]=Null

    front=(front+1) mod N

}





# Queue Implementation

- ▶ **Array:** We will use this first.
- ▶ **Linked Lists:** Later to be implemented with list.



# Lab Assignment

- ▶ Implement the **Queue** in C++ using OOP.

# Exercises

---

- Describe in pseudo-code an algorithm for reversing a queue  $Q$ . To access the queue, you are only allowed to use the methods of a queue ADT. **Hint:** Consider using an auxiliary data structure.

# Exercises

---

- A linear list of elements in which deletion can be done from one end (front) and insertion can take place only at the other end (rear) is known as a?
  - a) Queue.
  - b) Stack.
  - c) Tree.
  - d) Linked list.
- A queue follows
  - a) FIFO (First In First Out) principle.
  - b) LIFO (Last In First Out) principle.
  - c) Ordered array.
  - d) Linear tree.